



Cambridge International AS Level

MATHEMATICS

9709/22

Paper 2 Pure Mathematics 2

March 2021

MARK SCHEME

Maximum Mark: 50

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

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This document consists of **12** printed pages.

PUBLISHED**Generic Marking Principles**

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

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Mathematics Specific Marking Principles	
1	Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

PUBLISHED**Mark Scheme Notes**

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

- M** Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B** Mark for a correct result or statement independent of method marks.
- DM or DB** When a part of a question has two or more ‘method’ steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly, when there are several B marks allocated. The notation DM or DB is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- FT** Implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only.
- A or B marks are given for correct work only (not for results obtained from incorrect working) unless follow through is allowed (see abbreviation FT above).
 - For a numerical answer, allow the A or B mark if the answer is correct to 3 significant figures or would be correct to 3 significant figures if rounded (1 decimal place for angles in degrees).
 - The total number of marks available for each question is shown at the bottom of the Marks column.
 - Wrong or missing units in an answer should not result in loss of marks unless the guidance indicates otherwise.
 - Square brackets [] around text or numbers show extra information not needed for the mark to be awarded.

Abbreviations

AEF/OE	Any Equivalent Form (of answer is equally acceptable) / Or Equivalent
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
CAO	Correct Answer Only (emphasising that no ‘follow through’ from a previous error is allowed)
CWO	Correct Working Only
ISW	Ignore Subsequent Working
SOI	Seen Or Implied
SC	Special Case (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)
WWW	Without Wrong Working
AWRT	Answer Which Rounds To

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Question	Answer	Marks	Guidance
1(a)	Draw V-shaped graph with vertex on positive x -axis	B1	
	Draw correct graph of $y = x + 2$ with smaller positive gradient	B1	Crossing y -axis between 0 and y -intercept of first graph.
		2	
1(b)	Solve $3x - 5 = x + 2$ to obtain $x = \frac{7}{2}$	B1	
	Attempt solution of linear equation where signs of $3x$ and x are different.	M1	
	Obtain $x = \frac{3}{4}$	A1	
	Alternative method for question 1(b)		
	State or imply non-modulus equation $(3x - 5)^2 = (x + 2)^2$	B1	
	Attempt solution of 3-term quadratic equation	M1	
	Obtain $\frac{3}{4}$ and $\frac{7}{2}$	A1	
		3	

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Question	Answer	Marks	Guidance
2	State $\frac{1}{\cos^2 \theta} \times \frac{\cos \theta}{\sin \theta} = 8$	B1	OE involving $\sin \theta$ and $\cos \theta$ only.
	Attempt use of $\sin 2\theta$ identity to obtain $\sin 2\theta = k$	M1	
	Obtain $\sin 2\theta = \frac{1}{4}$	A1	
	Use correct process to find two values of θ between 0 and π	M1	Allow if working in degrees.
	Obtain 0.126 and 1.44	A1	AWRT
	Alternative method for question 2		
	State $\frac{1 + \tan^2 \theta}{\tan \theta} = 8$	B1	
	Attempt solution of 3-term quadratic equation to find values of $\tan \theta$	M1	OE involving $\tan \theta$ only.
	Obtain $\tan \theta = \frac{8 \pm \sqrt{60}}{2}$	A1	OE
	Solve $\tan \theta = \dots$ to find two values of θ between 0 and π	M1	Allow if working in degrees.
	Obtain 0.126 and 1.44	A1	AWRT
		5	

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Question	Answer	Marks	Guidance
3	Attempt use of product rule to find $\frac{dx}{dt}$	M1	
	Obtain $2e^{2t} \cos 4t - 4e^{2t} \sin 4t$	A1	
	Obtain $\frac{dy}{dt} = 6 \cos 2t$	B1	
	Divide to find $\frac{dy}{dx}$ with $t = 0$ substituted	M1	
	Obtain 3	A1	CWO
		5	

Question	Answer	Marks	Guidance
4(a)	Differentiate using quotient rule (or product rule)	M1*	
	Obtain $\frac{5(4x^3 + 1) - 60x^3}{(4x^3 + 1)^2}$	A1	OE
	Equate first derivative to zero and attempt solution	DM1	
	Obtain $x = \frac{1}{2}$	A1	
		4	

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Question	Answer	Marks	Guidance
4(b)	Use y values $\frac{5}{5}$, $\frac{10}{33}$, $\frac{15}{109}$ or decimal equivalents	B1	
	Use correct formula, or equivalent, with $h = 1$	M1	
	Obtain $\frac{1}{2} \left(1 + \frac{20}{33} + \frac{15}{109} \right)$ or equivalent and hence 0.87	A1	
		3	
4(c)	State over-estimate with reference to top of each trapezium above curve	B1	Or clear equivalent.
		1	

Question	Answer	Marks	Guidance
5(a)	Use the power law correctly	*M1	
	Use correct process to obtain equation with no logarithms	DM1	
	Confirm $x = \sqrt{\frac{9}{x+2}}$	A1	AG; condone absence of justification for choice of positive root.
		3	
5(b)	Consider sign of $x - \sqrt{\frac{9}{x+2}}$ or equivalent for 1.5 and 2	M1	
	Obtain -0.1... and 0.5 or equivalents and justify conclusion	A1	AG
		2	

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Question	Answer	Marks	Guidance
5(c)	Use iteration process correctly at least once	M1	
	Obtain final answer 1.58	A1	Final answer required to exactly 3 sf.
	Show sufficient iterations to 5 sf to justify answer or show a sign change in interval [1.575, 1.585]	A1	
		3	

Question	Answer	Marks	Guidance
6(a)	Substitute $x = -2$ and equate to zero	*M1	
	Substitute $x = 3$ and equate to 5	*M1	
	Obtain $-8 - 2a + b = 0$ and $27 + 3a + b = 5$ or equivalents	A1	
	Solve a pair of relevant linear simultaneous equations for a or b	DM1	Dependent at least one M mark.
	Obtain $a = -6$ and $b = -4$	A1	
		5	

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Question	Answer	Marks	Guidance
6(b)	Attempt division by $x + 2$ at least as far as $x^2 + kx$	M1	
	Obtain $x^2 - 2x - 2$	A1	
	Obtain (at least) the positive root $\frac{2 + \sqrt{12}}{2}$ or exact equivalent	A1	
	Equate e^{2y} to positive root, apply logarithms and use power law	M1	
	Obtain $\frac{1}{2} \ln \left(\frac{2 + \sqrt{12}}{2} \right)$ or $\frac{1}{2} \ln(1 + \sqrt{3})$ or exact equivalent	A1	
		5	

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Question	Answer	Marks	Guidance
7(a)	State $R = 10$	B1	
	Use appropriate trigonometry to find α	M1	
	Obtain $\alpha = \frac{1}{6}\pi$	A1	
		3	
7(b)	State -6	B1 FT	Following <i>their</i> value of R .
	Attempt to find x from their $\cos(x - \alpha) = -1$	M1	
	Obtain $x - \frac{1}{6}\pi = -\pi$ and hence $-\frac{5}{6}\pi$	A1	
		3	
7(c)	State integrand of form $k_1 \sec^2\left(3\theta - \frac{1}{6}\pi\right)$	*M1	
	Integrate to obtain form $k_2 \tan\left(3\theta - \frac{1}{6}\pi\right)$	DM1	
	Obtain $\frac{1}{300} \tan\left(3\theta - \frac{1}{6}\pi\right) + c$	A1	
		3	